



## Transport dynamic equations with impurity in tokamak plasmas

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The transport dynamics of various ions and electron in tokamak plasmas is a very important research area. Herein, on the basis of the non-equilibrium statistical theory, the transport equations of impurity ions, deuterium ion and electron were derived from Fokker-Planck kinetic equation. The transport dynamics of impurity ions with Zth-order charge which is forming in the various ionization levels and the explicitly collisions contribution between different particles are systematically analyzed in this work. The basic equations are re-derived and simplified on the basis of the previous works. Therefore, the transport equations of different particles in this system are concise and systematic.

$$\frac{\partial n}{\partial t} + \nabla \cdot (n\mathbf{u}) = S^N \quad (1)$$

$$\begin{aligned} \frac{\partial u_{\parallel}}{\partial t} + \mathbf{u} \cdot (\nabla u_{\parallel}) + \frac{\hat{\mathbf{b}}}{nm} \cdot (\nabla \cdot \tilde{\pi}) + \frac{\hat{\mathbf{b}}}{nm} \cdot [\nabla(nT)] \\ = \frac{Ze}{m} \hat{\mathbf{b}} \cdot \mathbf{E} + \frac{\hat{\mathbf{b}} \cdot \mathbf{R}}{mn} + \frac{\hat{\mathbf{b}} \cdot \mathbf{S}^M}{mn} - \frac{u_{\parallel}}{n} S^N \end{aligned} \quad (2)$$

$$\begin{aligned} \frac{3}{2} n \left[ \frac{\partial T}{\partial t} + \mathbf{u} \cdot (\nabla T) \right] + nT \nabla \cdot \mathbf{u} + \nabla \cdot (\tilde{\pi} \cdot \mathbf{u}) + \nabla \cdot \mathbf{q} \\ = Q + S^E - \mathbf{u}_{\parallel} \cdot \mathbf{S}^M + \left( \frac{1}{2} m u_{\parallel}^2 - \frac{3}{2} T \right) S^N + \mathbf{u}_{\parallel} \cdot (\nabla \cdot \tilde{\pi}) \end{aligned} \quad (3)$$

### References

- (1) S. I. Braginskii, in Reviews of Plasma Physics, edited by M. A. Leontovich (Consultants Bureau, New York, 1965), Vol. 1, p. 205.
- (2) A. N. Simakov and P. J. Catto, Plasma Phys. 10, 4744 (2003).
- (3) C. Bae, W. M. Stacey and W. M. Solomon, Nucl. Fusion 53, 043011 (2013).