

## Boris-type particle solvers in particle-in-cell (PIC) simulation

Seiji Zenitani<sup>1</sup>, Kato N. Tsunehiko<sup>2</sup>, Takayuki Umeda<sup>3</sup><sup>1</sup> Kobe University, <sup>2</sup> National Astronomical Observatory of Japan, <sup>3</sup> Nagoya University  
e-mail: zenitani@port.kobe-u.ac.jp

Particle-in-cell (PIC) simulation has long been used in theoretical plasma physics. In PIC simulation, the Boris solver is a de facto standard to advance charged particles, and it has been used for nearly 50 years. Meanwhile, there is a growing demand for better particle solvers, because scientists are carrying out longer simulations than ever, and because small errors will be accumulated in such long-time simulations.

In this contribution, we will introduce two particle solvers to advance charged particles in PIC simulation. First, we propose a particle solver that takes advantage of two exact solutions for the Coulomb-force part and for the Lorentz-force part [1]. It provides a second-order accuracy, and it gives much more accurate results than a popular form of the Boris solver. Second, we propose a family of approximate Boris-type solvers [2]. They virtually repeat the popular form of Boris solver multiple times ( $n$  times), and their one-step forms are provided by using Chebyshev polynomials.

We compare accuracy and computation time of Boris-type solvers, including our new solvers, by means of test-particle simulations. For example, Figure 1 presents numerical errors by various solvers as a function of the timestep  $\Delta t$ . One can see that our exact-type (Zenitani=Umeda) solver is as good as the Boris solver with gyrophase correction. We also evaluate particle solvers in a magnetized flow at a relativistic speed [3].

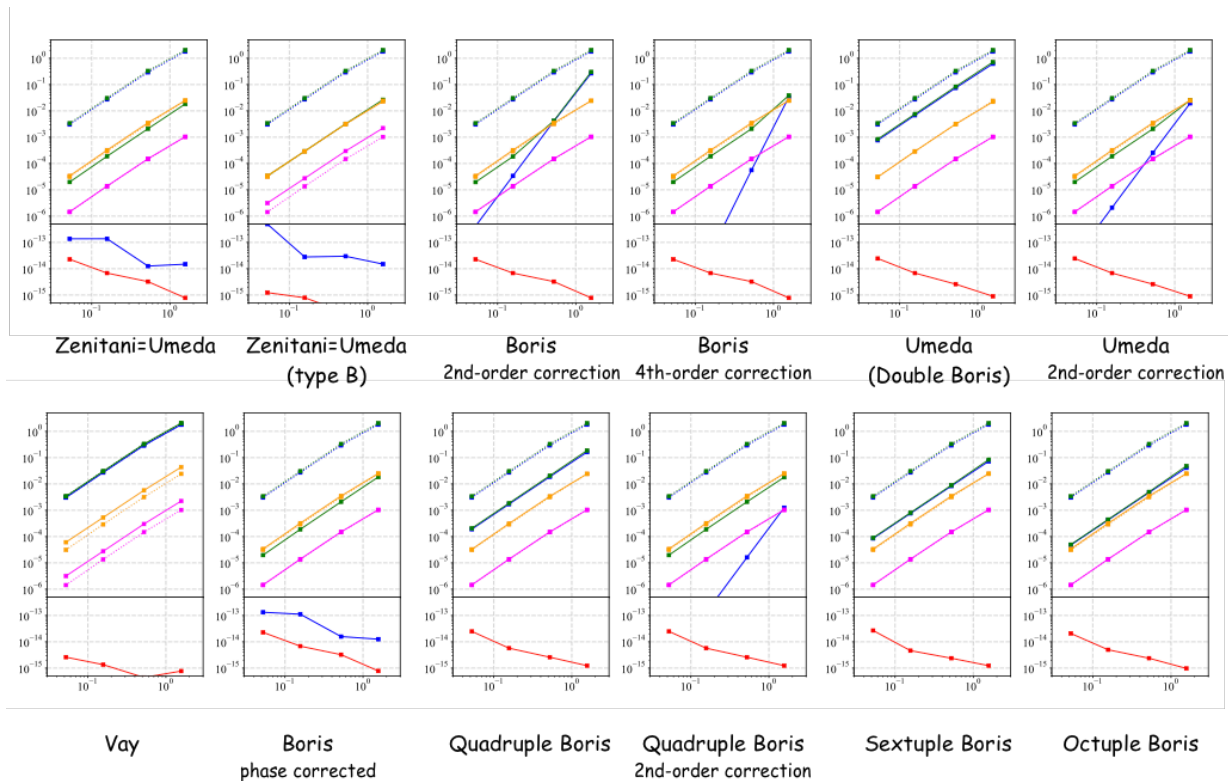


Figure 1. Numerical errors in test-particle simulations by various particle solvers. The vertical axis shows normalized numerical errors, the horizontal axis shows the timestep  $\Delta t$ , and the color indicates field configurations in the same format as in Figure 2 in Ref. [1]. The solid lines indicate the results by each solver, while the dotted lines indicate the results by the popular form of the Boris solver.

### References

1. S. Zenitani & T. Umeda, *On the Boris solver in particle-in-cell simulation*, *Physics of Plasmas* **25**, 112110, <https://doi.org/10.1063/1.5051077> (2018)
2. S. Zenitani & T. N. Kato, *Multiple Boris integrators for particle-in-cell simulation*, submitted to *Comput. Phys. Commun.* (2019)
3. S. Zenitani & T. N. Kato, *Numerical methods for charged particles in relativistic particle-in-cell simulation*, *Sustainable Humanosphere* **14**, 62, <http://hdl.handle.net/2433/235378> (2018) (in Japanese language)