

# Numerical Simulation of Ion-Based Water-Window Harmonic Generation in Laser-Irradiated Gases

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High-harmonic generation (HHG) induced in laser-irradiated atomic or molecular gases is an important method to generate water-window soft X-ray. The focused laser pulse ionizes the gas medium, and the released electrons undergo the acceleration and recombination processes to emit short-wavelength photons [1]. The figure of merits to characterize the performance of HHG are the cutoff photon energy and the conversion efficiency.

The cutoff photon energy of HHG  $E_c$  can be derived that  $E_c = I_p + 3.17U_p$ , where  $I_p$  is the ionization potential, and  $U_p$  is the ponderomotive energy. In order to increase  $E_c$ , e.g. water-window X-ray range, ion species is a better HHG emitters. Ion has higher ionization potential than atom, cause the higher cutoff energy. In addition, with higher  $I_p$ , the ions can only be ionized under a higher laser intensity, which increase  $U_p$ . Based on the above conditions, we choose He as our neutral gas target, and generate the high harmonic by He and He<sup>1+</sup>.

The conversion efficiency of HHG is mainly determined by the phase-matching condition of the generation process. It is determined by four mechanisms, i.e., neutral gas dispersion, plasma dispersion, geometrical phase shift (Gouy phase shift), and intensity-dependent dipole phase variation. Moreover, using a shorter wavelength driving laser can also enhance the conversion efficiency, since the single-atom response scales with  $\sim \lambda^{-6}$  between interactions of different laser wavelengths with the same atom [2]. However, in the highly-ionized plasma regime, which represents high density HHG source, plasma dispersion is hardly to be balanced. Therefore, the phase-matching condition is difficult to be achieved, such that generation of high efficiency HHG at short wavelength becomes a big challenge.

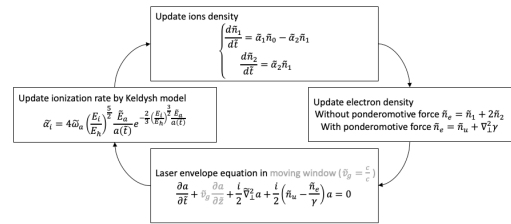
In this paper, we perform a numerical simulation of the ion-based HHG. We found that phase-matching condition can be achieved for water-window x-ray emission driven by 405-nm femtosecond pulses. We first apply the 3+1-dimensional hybrid advective-diffusion electromagnetic (EM) envelope equation with cylindrical symmetry, together with Keldysh's optical-field ionization model, to resolve the propagation of the driving pulse in a He gas target. The moving-window algorithm is adapted while solving the equation, as shown in Figure 1. Then we can have the ion/electron density distributions and calculate the phase-matching condition and the HHG yield.

The driving pulse specification is optimized to 16.5-mJ energy, 405-nm wavelength, and 30-fs duration. It is focused to a waist radius of 30  $\mu\text{m}$  at  $z = 0$ . The Helium gas is located between  $z = 7 \text{ mm}$  and  $z = 10 \text{ mm}$ , with a uniform density distribution  $1.8 \times 10^{17} \text{ cm}^{-3}$ . The resulted laser intensity, gas density, and electron density

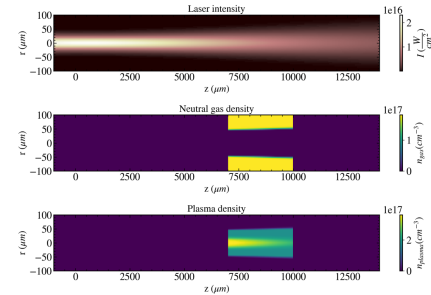
in  $z$ - $r$  space are shown in Figure 2. The phase-matching condition is achieved for the 93rd-order harmonic (4.35 nm) on the propagation axis ( $r = 0$ ), as shown in Figure 3. The 4.35-nm output yield generated through the processes of  $\text{He} \rightarrow \text{He}^{1+} \rightarrow \text{He}$  and  $\text{He}^{1+} \rightarrow \text{He}^{2+} \rightarrow \text{He}^{1+}$ , as well as the total HHG yield, are accumulated constructively within the entire interacting region.

## References

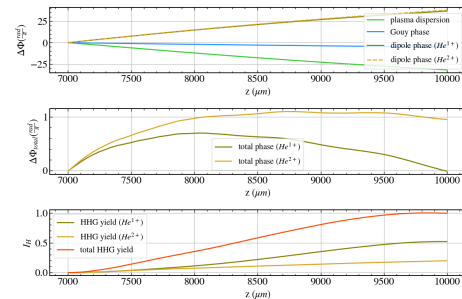
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**Figure 1.** Schematic illustration of the numerical algorithm.  $\tilde{n}$  is the normalization density and  $a$  is the normalization wave vector amplitude.



**Figure 2.** Simulation results show spatial profiles of laser intensity, helium gas density and electron density in  $z$ - $r$  space.



**Figure 3.** Phase matching condition and HHG yield varies along the propagation axis ( $r = 0$ ).